Challenge 120: Triangle Time

The hour hand on a clock is 3cm long and the minute hand is 5cm long. At certain times of day, the hands form two sides of a right-angled triangle.

In a 24 hour period, how many times will this happen?

For what proportion of these times does the right angled triangle that is formed have integer length sides?